

Topic: Electromagnetic Induction: [4M]

* Faraday's law:

Induced e.m.f. $\epsilon = \frac{d\phi}{dt}$ [rate ofchange of magnetic flux
associated with coil.(*) Lenz's law: The direction of induced
e.m.f. is such that it tries to
oppose the change in magnetic flux
which produce it. $\epsilon = - \frac{d\phi}{dt}$

(*) Coefficient of self induction.

$$L = \frac{\epsilon}{di/dt}.$$

S.I unit: Henry (H)

Dimension:

$$[L^2 M^1 T^{-2} I^{-2}]$$

(*) Coefficient of mutual induction.

$$M = \frac{\epsilon_s}{di/dt}.$$

It is the phenomenon of production
of an induced e.m.f. in one coil
due to change of current in neighbouring
coil.

Unit: henry [H]

Dimension:

$$[L^2 M^1 T^{-2} I^{-2}]$$

(*) Transformer:

(1) Step-up transformer.

$$N_s > N_p \quad \text{also} \quad \epsilon_s > \epsilon_p.$$

(2) Step-down transformer.

$$N_s < N_p$$

$$\epsilon_s < \epsilon_p$$

(*) Transformer ratio

$$\frac{E_s}{E_p} = \frac{N_s}{N_p}$$

(*) Coil rotating in a uniform magnetic field.

$$e = - \frac{d\phi}{dt} = - \frac{d}{dt} (NAB \cos \omega t)$$

$$e = NAB \omega \sin \omega t$$

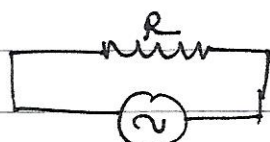
$$e = e_0 \sin \omega t$$

$$\omega = 2\pi f, \quad e_0 = NAB\omega =$$

(*) $i_{r.m.s.} = \frac{i_0}{\sqrt{2}} = 0.7071 i_0$

$e_{r.m.s.} = \frac{e_0}{\sqrt{2}} = (0.7071) e_0$

(*) A.C. circuit with resistor.



$$i = \frac{e}{R} = \frac{e_0}{R} \sin \omega t$$

$$e = e_0 \sin \omega t, \quad i = i_0 \sin \omega t$$

Phase angle $\phi = 0$.

Power factor $\cos \phi = 1$.

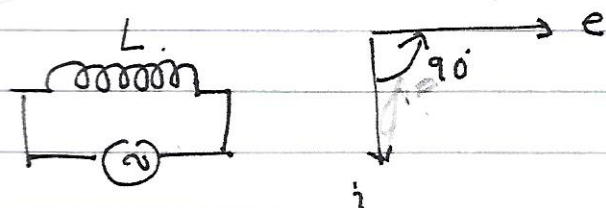
Instantaneous Power $P = e i$
 $= (e_0 \sin \omega t)(i_0 \sin \omega t)$
 $= e_0 i_0 \sin^2 \omega t$

Average or mean Power

$$P_{av} = i_{r.m.s.} \times e_{r.m.s.}$$

$$= \frac{i_0}{\sqrt{2}} \times \frac{e_0}{\sqrt{2}} = \frac{P_0}{2} = \frac{e_0 i_0}{2}$$

(*) Simple A.C. circuit with pure Inductance (L).



$$i = i_0 \sin \omega t.$$

$$e_{\text{back}} = -L \frac{di}{dt} = \omega L i_0 \cos \omega t.$$

$$e_{\text{max}} = \omega L i_0 = e_0.$$

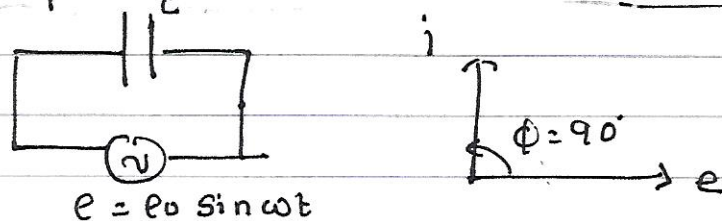
(i) $e = e_0 \cos \omega t.$

(ii) Inductive reactance $X_L = \omega L = \frac{e_{\text{r.m.s.}}}{i_{\text{r.m.s.}}}$

(iii) Power factor $= \cos \phi = 0.$

(iv) Phase angle: e.m.f. leads current by $\pi/2$

(*) 1 Simple A.C. circuit with pure capacitance:



$$e = e_0 \sin \omega t.$$

$$\frac{q}{C} = e_0 \sin \omega t.$$

$$\frac{dq}{dt} = C e_0 \frac{d}{dt} (\sin \omega t).$$

$$i = \omega C e_0 \cos \omega t.$$

(b) $i = i_0 \cos \omega t.$

$$i_{\text{max}} = i_0 = \omega C e_0.$$

(c) capacitive reactance $= X_C = \frac{1}{\omega C} = \frac{e_0}{i_0}$

$$= \frac{e_0 / \sqrt{2}}{i_0 / \sqrt{2}} = \frac{e_{r.m.s.}}{i_{r.m.s.}}$$

(3) Power factor $= \cos \phi = 0$

(4) Phase angle: e.m.f. across the capacitor lags behind the current by phase angle of $\pi/2$

(*) An alternating current LCR series circuit:

(1) $E = i \sqrt{R^2 + (X_L - X_C)^2}$

$$E = i Z$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \text{ — Impedance (}\Omega\text{)}$$

(ii) Phase angle ϕ , $\tan \phi = \frac{X_L - X_C}{R}$

(iii) Power factor $= \cos \phi = \frac{R}{Z} = \frac{\text{Resistance}}{\text{Impedance}}$

(iv) At resonance,

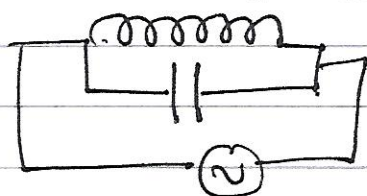
$$X_L = X_C$$

$$\omega L = \frac{1}{\omega C}$$

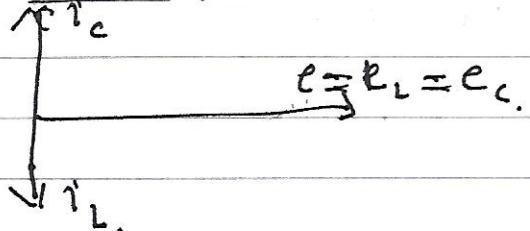
$$\omega = \frac{1}{\sqrt{LC}}$$

$$f = \frac{1}{2\pi \sqrt{LC}}$$

(*) Parallel resonant circuit:



Circuit:



$$i_L = \frac{e}{X_L}$$

$$i_C = \frac{e}{X_C}$$

$$V = e \left(\frac{1}{X_C} - \frac{1}{X_L} \right)$$

$$= e \left(\frac{1}{1/\omega C} - \frac{1}{\omega L} \right)$$

$$= e \left(\omega C - \frac{1}{\omega L} \right)$$

$$Z = \frac{e}{i} = \frac{1}{(\omega C - \frac{1}{\omega L})}$$